

AUTOMATIC GENOTYPE DETERMINATION

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AUTOMATIC GENOTYPE DETERMINATION

Cross Reference to Related Applications

Ans 1 This application is a continuation of application serial no. 08/362,266, filed December 22, 1994, which is a continuation in part of application serial no. 08/173,173, filed December 23, 1993, which is for an invention entitled "Automatic Genotype Determination," by Stephen E. Lincoln and Michael P. Knapp. This immediate parent application is a continuation in part of application serial no. 07/775,786, filed October 11, 1991, for an invention entitled "Nucleic Acid Typing by Polymerase Extension of Oligonucleotides using Terminator Mixtures," by P. Goelet, M. Knapp, and S. Anderson, which in turn is a continuation in part of application serial no. 07/664,837, filed March 5, 1991. Immediate parent application serial no. 08/173,173 is also a continuation in part of application serial no. 08/162,397, filed December 6, 1993, for an invention entitled "Method for Immobilization of Nucleic Acid Molecules" by T. Nikiforov and M. Knapp, and of application serial no. 08/155,746, filed November 23, 1993, for an invention entitled "Method for Generating Single-Stranded DNA Molecules" by T. Nikiforov and M. Knapp, and of application serial no. 08/145,145, filed November 3, 1993, for an invention entitled "Single Nucleotide Polymorphisms and their use in Genetic Analysis" by M. Knapp and P. Goelet. All of these related applications are hereby incorporated herein by reference.

Technical Field

The present invention relates to the methods and devices for determining the genotype at a locus within genetic material.

Summary of the Invention

The present invention provides in one embodiment a method of determining the genotype at a locus within genetic material obtained from a biological sample. In accordance with this method, the material is reacted at the locus to produce a first reaction value indicative of the presence of a given allele at the locus. There is formed a data set, including the first reaction value. There is also established a set of one or more probability distributions; these distributions associate hypothetical reaction values with corresponding probabilities for each genotype of interest at the locus. The first reaction value is applied to each probability distribution to determine a measure of the conditional probability of each genotype of interest at the locus. The genotype is then determined based on these measures.

In accordance with a further embodiment of this method, the material at the locus is subject to a second reaction to produce a second reaction value independently indicative of the presence of a second allele at the locus. A second data set is formed and the second reaction value is included in the second data set. Each probability distribution associates a hypothetical pair of first and second reaction

5 values with a single probability of each genotype of
interest. The first data set includes other reaction values
obtained under conditions comparable to those under which
the first reaction value was produced, and the second data
set includes other reaction values obtained under conditions
10 comparable to those under which the second reaction value
was produced. Where, for example, there are two alleles of
interest, the first reaction may be an assay for one allele
and the second reaction may be a distinct assay for the
other allele. The first and second data sets may include
reaction values for the first and second reactions
respectively, run under comparable conditions on other
samples with respect to the same locus. Alternatively, or in
addition, the data sets may include reaction values for
reactions run under comparable conditions with respect to
different loci within the same sample.

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25 In accordance with a further embodiment, the
probability distributions may be determined iteratively. In
this embodiment, each probability distribution is initially
estimated. Each initial probability distribution is used to
determine initial genotype probabilities using the reaction
values in the data sets. The resulting data are then used to
modify the initial probability distribution, so that the
modified distribution more accurately reflects the reaction
values in the data set. This procedure may be iterated a
30 desired number of times to improve the probability
distribution. In practice, we have generally found that a
single iteration is sufficient.

5 The foregoing methods have been employed with success
for automatic genotype determination based on assays using
genetic bit analysis (GBA). In such a case, each allele may
typically be a single specific nucleotide. In accordance
with GBA, a reaction is designed to produce a value that is
10 indicative of the presence of a specific allele at the locus
within the genetic material. In GBA, the approach is
typically to hybridize a specific oligonucleotide to the
genetic material at the locus immediately adjacent to the
nucleotide being interrogated. Next, DNA polymerase is
applied in the presence of differentially labelled
dideoxynucleoside triphosphates. The read-out steps detect
the presence of one or more of the labels which have become
covalently attached to the 3' end of the oligonucleotide.
Details are provided in Theo R. Nikiforov et al. "Genetic
Bit Analysis, a solid phase method for typing single
nucleotide polymorphisms," 22 Nucleic Acids Research, No.
20, 4167-4175 (1994), which is hereby incorporated herein by
reference. However, the present invention is also applicable
to other reaction systems for allele determination, such as
25 allele-specific hybridization (ASH), sequencing by
hybridization (CBH), oligonucleotide ligase assay (OLA), and
allele-specific amplification, using either the ligase chain
reaction (LCR) or the polymerase chain reactions (PCR). The
alleles assayed may be defined, for example, by a single
30 nucleotide, a pair of nucleotides, a restriction site, or
(at least in part) by its length in nucleotides.

In another embodiment of the invention, there is

5 at the locus. Thereafter the distribution establishment arrangement modifies each initial probability distribution, so that each modified distribution more accurately reflects the reaction values stored in the storage means.

10 The term "reaction value" as used in this description and the following claims may refer either to a single numerical value or to a collection of numbers associated with a physical state produced by the reaction. In the GBA method described in the Nikiforov article referred to above, e.g., optical signals are produced that may be read as a single numerical value. Alternatively, e.g., an optical signal may be simplified over time, and the reaction value may be the collection of samples of such a signal. It is also possible to form a scanned image, of one or a series of optical signals generated by GBA or other reaction methods, and to digitize this image, so that a collection of pixel values in all or a portion of the image constitutes a reaction value.

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Brief Description of the Drawings

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The foregoing aspects of the invention will be more readily understood by reference to the following detailed description, taken with respect to the following drawings, in which:

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Fig. 1 is a diagram of a device in accordance with a preferred embodiment of the invention;

Fig. 2 is a diagram of the logical flow in accordance

5 obtained under comparable conditions. A distribution establishment arrangement establishes a set of probability distributions, including at least one distribution, associating hypothetical reaction values with corresponding probabilities for each genotype of interest at the locus. A 10 genotype calculation arrangement applies the first reaction value to each pertinent probability distribution to determine the conditional probability of each genotype of interest at the locus. A genotype determination arrangement determines the genotype based on data from the genotype calculation arrangement.

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In a further embodiment, the device may determine the genotype at selected loci. In this embodiment, the reaction generation arrangement can produce a reaction value indicative of the presence of a given allele at each of the selected loci and the data set includes reaction values obtained with respect to each of the selected loci. The genotype calculation arrangement applies reaction values obtained with respect to each of the selected loci to each pertinent probability distribution.

25 In another further embodiment, the device may determine the genotype at a locus within genetic material from each of a plurality of samples. In this embodiment, the reaction generation arrangement can produce a reaction value indicative of the presence of a given allele at the locus of material obtained from each sample and the data set includes reaction values obtained with respect to each sample. The 30 genotype calculation arrangement applies reaction values

5 obtained with respect to each sample to each pertinent probability distribution.

In each of these embodiments the reaction value generation arrangement may also include an arrangement for producing a second reaction value, independently indicative 10 of the presence of a second allele at the locus. The storage arrangement then includes a provision for storing the second reaction value and other reaction values obtained under comparable conditions. The genotype calculation arrangement applies the first and second reaction values to each pertinent probability distribution to determine the probability of each genotype of interest at the locus. Each probability distribution may be of the type associating a hypothetical pair of first and second reaction values with a single probability of each genotype of interest. The locus may be a single nucleotide, and the reaction value generation arrangement may include an optical transducer to read reaction results and may determine, on a substantially concurrent basis, the reaction values with respect to each sample.

25 The distribution establishment arrangement may be configured to assign an initial probability distribution to the data set that would associate hypothetical reaction values with corresponding probabilities for each genotype of interest at the locus. The distribution establishment arrangement then invokes the genotype calculation means to use each initial probability distribution to determine 30 initial conditional probabilities for a genotype of interest

5 provided a method of determining the genotype of a subject
by reacting genetic material taken from the subject at
selected loci. In this embodiment, each locus may be an
identified single nucleotide or group of nucleotides, and
there is produced with respect to each of the selected loci
10 a reaction value indicative of the presence of a given
allele at each of the selected loci. These reaction values
are used to determine the genotype of the subject or
alternatively a DNA sequence associated with a specific
region of genetic material of the subject. (Indeed a set of
15 genotypes for selected proximal loci may be used to specify
a sequence of the genetic material.). In further embodiments,
the loci are selected to provide one or more types of
information concerning the subject, including inheritance of
20 a trait, parentage, identity, and matching tissue with that
of a donor. Alternatively, the loci may be spaced
throughout the entire genome of subject to assist in
characterizing the genome of the species of the subject.

In a further embodiment of the invention, there is provided a device for determining the genotype at a locus within genetic material obtained from a subject. The device of this embodiment has a reaction value generation arrangement for producing a first physical state, quantifiable as a first reaction value, indicative of the presence of a given allele at the locus, the value associated with reaction of the material at the locus. The device also has a storage arrangement for storing a data set including the first reaction value and other reaction values

5 with the embodiment of Fig. 1;

Fig. 3 is a graph of numeric reaction values (data) generated by the embodiment of Fig. 1 as well as the genotype determinations made by the embodiment from these data; and

10 Figs. 4-7 show probability distributions derived by the embodiment of Fig. 1 for three genotypes of interest (AA, AT, and TT) and a failure mode at a locus.

Fig. 8 is an example of the output of the device in Fig. 1.

Detailed Description of Specific Embodiments

The invention provides in preferred embodiments a method and device for genotype determination using genetic marker systems that produce allele-specific quantitative signals. An embodiment uses computer processing, employing computer software we developed and call "GetGenos", of data produced by a device we also developed to produce GBA data. The device achieves, among other things, the following:

25 • Fully automatic genotype determination from quantitative data. Off-line analysis of data pools is intended, although the software is fast enough to use interactively.

30 • Ability to examine many allele tests per DNA sample simultaneously. One genotype and confidence measure are produced from these data.

• A true probabilistic confidence measure (a LOD

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5 score), properly calibrated, is produced for each genotype.

- Use of robust statistical methods: Noise reduction via selective data pooling and simultaneous search over points in a data pool, preventing bias.

10 • Maximal avoidance of arbitrary parameters, and thus insensitivity to great variation in input data. The small number of parameters that are required by the underlying statistical model are fit to the observed data, essentially using the data set as its own internal control.

15 • Flexibility for handling multiple data types. Essentially, only probability distribution calculations, described below, need to be calibrated to new data types. We expect that the invention may be applied to GBA, OLA, ASH, and RAPD-type markers.

Our current embodiment of the software is implemented in portable ANSI C, for easy integration into a custom laboratory information system. This code has been successfully run on:

- Macintosh
- Sun
- MS-DOS
- MS-Windows

25 In our current embodiment of the software, a number of consistency checks are performed for GBA data verification, using both the raw GBA values and the control wells.

30 Overall statistics for trend analysis and QC are computed. Brief "Genotype Reports" are generated, summarizing results for each data set, including failures. All data are output

5 in a convenient form for import into interactive statistical packages, such as DataDesk™. The current implementation is presently restricted to 2-allele tests in diploids - the situation with present GBA applications.

10 Referring to Fig. 1, there is shown a preferred embodiment of a device in accordance with the present invention. The device includes an optical detector 11 to produce reaction values resulting from one or more reactions. These reactions assay for one or more alleles in samples of genetic material. We have implemented the detector 11 using bichromatic microplate reader model 348 and microplate stacker model 83 from ICN Biomedical, Inc., P.O. Box 5023, Costa Mesa, California 92626. The microplates are in a 96 well format, and the reader accommodates 20 microplates in a single processing batch. Accordingly the device of this embodiment permits large batch processing. The reactions in our implementation use GBA, as described above. The detector 11 is controlled by computer 12 to cause selected readout of reaction values from each well. The computer 12 is programmed to allow for multiple readout of the reaction value from a given well over a period of time. The values are stored temporarily in memory and then saved in database 14. Computer 13 accesses the database 14 over line 15 and processes the data in accordance with the procedure described below. Of course, computers 12 and 13 and database 14 may be implemented by an integral controller and data storage arrangement. Such an arrangement could in fact be located in the housing of the optical detector 11.

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5 In Fig. 2 is shown the procedure followed by computer
13. The steps of this procedure are as follows:

10 Input Data: A set of data is loaded under step 21. In
most applications, each experiment in the set should be
testing (i) the same genetic marker, and (ii) the same set
of alleles of that marker, using comparable biochemistry
(e.g. the same reagent batches, etc.). Large data sets help
smooth out noise, although the appropriate size of a data
set depends on the allele frequencies (and thus the number
of expected individuals of each genotypic class). Each data
point in the input data may be thought of as an N -tuple of
numeric values, where N is the number of signals collected
from each DNA sample for this locus. (N will usually be the
number of alleles tested at this marker, denoted A , except
when repeated testing is used, in which case N may be
greater than A).

25 Preprocess Data: Next the data are subject to
preprocessing (step 22). An internal M -dimensional Euclidean
representation of the input signals is produced, where each
input datum (an N -tuple) is a point in M -space. Usually, M
will be the same as N and the coordinates of the point will
be the values of the input tuple, and thus the preprocessing
will be trivial (although see the first paragraph of
variations discussed). The Euclidean space may be
non-linear, depending on the best available models of signal
30 generation. (Completely mathematically equivalently, any
non-linearity may be embodied in the initial probability
distributions, described below.)

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5 Fig. 3 illustrates preprocessed reaction values from
 step 22 for GBA locus 177-2 on 80 DNA samples. The X-axis
 indicates preprocessed reaction values for allele 1 (A) and
 the Y-axis indicates preprocessed reaction values for allele
 10 2 (T). For clarity, the results of genotype determination
 are also indicated for each point: Triangles are TT
 genotype, diamonds are AA, circles are AT, and squares are
 failures (no signal).

Probability Distributions: Returning to Fig. 2, under
 step 22, initial probability distributions are established
 for the G possible genotypes. For example, in a random
 diploid population containing A tested alleles:

$$G = (A) + (A - 1) + \dots + 1 = \frac{A(A + 1)}{2} \quad (1)$$

20 The initial conditional probability for any hypothetical
 input datum (a point in M -space, denoted x_i) and genotype
 (denoted g) is defined as the prior probability of seeing
 the signal x_i assuming that g is the correct genotype of
 25 that datum. That is:

$$\Pr(\text{signal } x_i \cdot \text{Genotype} = g), \\ \text{where } x_i = (x_i^1 \dots x_i^M) \text{ and } g \in \{1 \dots G\} \quad (2)$$

30 Figures 4 through 7 illustrate the initial probability
 distributions established for the data in figure 3.
 Probability distributions are indicated for the four

5 genotypic classes of interest, AA, AT, TT and No Signal, in
 Figs 4, 5, 6, and 7 respectively. The shading at each XY
 position indicates probability, with darker shades
 indicating increased probability for hypothetical data
 points with those X and Y reaction valves.

10 Exactly where these distributions come from is highly
 specific to the nature of the input data. The probability
 distributions can either be pre-computed at this step and
 stored as quantized data, or can be calculated on the fly as
 needed in step 23, below. The probability distributions may
 be fixed, or may be fit to the observed data or may be fit
 to assumed genotypes as determined by previous iterations of
 this algorithm. (See Additional Features below.)

15 Under step 23, we compute the conditional probability
 of each genotype. For each datum X_i , the above probabilities
 are collected into an overall conditional posterior
 probability of each genotype for that datum:

$$\Pr(\text{Genotype} = g \mid \text{Signal } X_i) = \frac{\Pr(\text{Signal } X_i \mid \text{Genotype} = g) \cdot \Pr(\text{Genotype} = g)}{\Pr(\text{Signal } X_i)} \quad (3)$$

20 where

25 $\Pr(\text{Genotype} = g)$ is the prior probability of any datum
 having genotype g ;

30 $\Pr(\text{Signal } X_i)$ is the prior probability of the signal (a
 constant which may be ignored); and

$\Pr(\text{Signal } X_i \mid \text{Genotype} = g)$ is the initial
 probability defined above.

5 Under step 24, we determine the select the genotype and
 compute the confidence score. For each datum, using the
 above posterior probabilities, we determine the most likely
 genotype assignment g' (the genotype with the highest
 posterior probability) and its confidence score. The
 10 confidence score C is simply the log of the odds ratio:

$$C = \log_{10} \frac{\Pr(\text{Genotype} = g' \mid \text{Signal } x_i)}{\sum_{\text{Genotypes } g} \Pr(\text{Genotype} = g \cdot \text{Signal } x_i)} \quad (4)$$

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 It should be noted that this procedure is significant, among
 other reasons, because it permits determining a robust
 probabilistic confidence score associated with each genotype
 determination.

20 Under step 25, there may be employed adaptive fitting.
 A classic iterative adaptive fitting algorithm, such as
 Estimation-Maximization (E-M), may be used to increase the
 ability to deal with highly different input data sets and
 reduce noise sensitivity. In this case, the genotypes
 25 computed in step 24 are used to refit the distributions
 (from step 22). In step 25, a convergence test is performed,
 which may cause the program to loop back to step 23, but now
 using the new distributions.

30 As one example, an E-M search procedure may be used to
 maximize the total likelihood, that is, to find the
 maximally likely set of genotype assignments given the input
 data set. (The net likelihood may be calculated from the
 Baysean probabilities, defined above.) For appropriate

5 likelihood calculations and probability distributions, the EM principle will guarantee that this algorithm always produces true-maximum-likelihood values, regardless of initial guess, and that it always converges.

10 Output Data: Under step 26, we output the results (genotypes and confidence scores) to the user or to a computer database. An example of such output is shown in Fig. 8.

Additional Features

15 Additional features may be incorporated into the above procedure. They may be integrated into the procedure either together or separately, and have all been implemented in a preferred embodiment.

20 Preprocessing: During steps 21 or 22, the data (either input tuples or spatial data points) may be preprocessed in order to reduce noise, using any one of many classical statistical or signal-processing techniques. Control data points may be used in this step. In fact, various types of signal filtering or normalizing may be applied at almost any step in the algorithm.

25 Fitting Probability Distributions: The probability distributions calculated in steps 22 and 23 may be fit to the input data - that is, each distribution may be a function of values which are in part calculated from the input data. For example, we may define the conditional probability of a signal point for some genotype to be a function of the distance between that point and the observed mean for that signal.

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5 Using an Initial Genotype Guess: In step 22, either a simple or heuristic algorithm may be used to produce an initial genotype guess for each input data point. If a fairly accurate guess can be produced, then the probability distributions for each genotype may be fit to the subset of
10 the data assumed to be of that genotypic class. Another use of a genotype guess is in initial input validity checks and/or preprocessing (e.g. Step 22), before the remainder of the algorithm is applied. To be useful, a guess need not produce complete genotypic information, however.

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Using a Null Genotypic Class: In steps 22 and all further steps, one (or more) additional probability distributions may be added to fit the data to the signals one would expect to see if an experiment (e.g. that datum) failed. E.g.,

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Using a Null Genotypic Class: In steps 22 and all further steps, one (or more) additional probability distributions may be added to fit the data to the signals one would expect to see if an experiment (e.g. that datum) failed. E.g.,

Pr (signal X_i • Genotype • {1 ... G})

The current implementation above is presently restricted to $M=2$ and $N=2*R$, where R is the number of repeated tests of both alleles. We refer to the two alleles as X and Y . The program understands the notion of "plates" of data, a number of which make up a data set.

The Initial Guess Variation is employed to initially fit distributions using the heuristic described below. The Initial Guess is produced during the Preprocessing Step which normalizes and background subtracts the input data, and remove apparent outlier points as well. These steps are

5 performed separately for each allele's signal (i.e., 1
dimensional analysis). In fact, this preprocessing is
applied separately to each of the R repeated tests, and the
test with the small total 2 dimension residual is chosen for
use in further steps. Various other preprocessing and
10 post-processing steps are employed for GBA data validation
and QC. In particular, controls producing a known reaction
value may be employed to assure integrity of the biochemical
process. In a preferred embodiment, signals are assumed to
be small positive numbers (between 0.0 and 5.0, with 0.0
15 indicating that allele is likely not present in the sample,
and larger values indicating that it may be.

To handle a wide range of input data signal strengths, the Adaptive Fitting Variation is employed. However, the program is hard-coded to perform exactly one or two interactions passes through step 25, which we find works well for existing GBA data.

Q The probability distributions we fit at present in
steps 22 and 25 have as their only parameters (i) the ratio
of the X and Y signals for heterozygotes, and (ii) the
variance from the normalized means (0.0 negative for that
allele, 1.0 for positive for that allele) along each axis
separately. In fact, these later numbers are constrained to
be at least a fixed minimum, which is rarely exceeded, so
that the algorithm will work with very small quantities of
data and will produce the behavior we want. These numbers
are computed separately for each microtiter plate. The
probability distributions are generated using the code

5 (written in C) attached hereto and incorporated herein by reference as Appendix A.

The Null-Class variant is used to provide genotypic class indicating No Signal.

10 Quality control may also be enhanced in a surprising manner using the procedures described here. In particular, the confidence score C of equation (4) serves as a robust indicator of the performance of the biochemical reaction system. For example, a downward trend in the confidence scores within a single batch or in successive batches may indicate deterioration of an important reagent or of a sample or miscalibration of the instrumentation.

15 Accordingly, in a preferred embodiment, the computer may be used to determine the presence of a downward trend in the confidence score over time calculated in reference to each of the following variables: the locus (is there a downward trend in the confidence score of a single locus relative to other loci tested?), the sample (is there a downward trend in the confidence score of a single sample relative to other samples tested?), plate (is there a downward trend in the confidence score of this plate relative to other plate?), and batch (relative to other batches). If a downward trend of statistical significance (using, for example a chi square test) is detected, an alarm condition is entered.

20 Because the confidence score is an accurate indication of the reliability of the reaction system and the genotype determination, a low confidence score associated with a

5 given determination is taken as indicating the need for retesting.

APPENDIX A

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/* The probability distributions in Figures 4, 5, 6, and 7, respectively,
correspond to the values of xx_prob, xy_prob, yy_prob, and ns_prob, for
all possible values of the preprocessed reaction values (x_val and y_val)
in the range of interest (0.0 to 3.0). */

/* We assume that the following global variables are set... */
double x_pos_mean, x_neg_mean, y_pos_mean, y_neg_mean;
double x_val, y_val;

/* And we set the following globals... */
double xx_prob, xy_prob, yy_prob, ns_prob;

#define POS_VARIANCE          0.25
#define POS_VARIANCE_INCREMENT 0.00
#define NEG_VARIANCE          0.05
#define NEG_VARIANCE_INCREMENT 0.10
#define HET_VARIANCE          0.10
#define HET_VARIANCE_INCREMENT 0.20

#define COND_NEG_PROB(val,given_val,val_mean) \
    normal_prob(val_mean-val,NEG_VARIANCE NEG_VARIANCE_INCREMENT*given_val)

#define COND_HET_PROB(val,given_val) \
    normal_prob(given_val-val,HET_VARIANCE + HET_VARIANCE_INCREMENT)

double normal_prob(deviation,sigma)
double deviation, sigma;
{
    double val=exp(-(deviation*deviation)/(2.0*sigma*sigma));
    return(val>=TINY_PROB ? val : TINY_PROB);
}

void compute_probs()
{
    double x_pos_prob, y_pos_prob, x_neg_prob, y_neg_prob;

    x_pos_prob=normal_prob((x_pos_mean-x_val), POS_VARIANCE);
    x_neg_prob=normal_prob((x_neg_mean-x_val), NEG_VARIANCE);
    y_pos_prob=normal_prob((y_pos_mean-y_val), POS_VARIANCE);
    y_neg_prob=normal_prob((y_neg_mean-y_val), NEG_VARIANCE);

    ns_prob=max(x_neg_prob * COND_NEG_PROB(y_val,x_val,y_neg_mean),
                y_neg_Prob * COND_NEG_PROB(x_val,y_val,x_neg_mean));

    xx_prob=x_pos_prob * COND_NEG_PROB(y_val,x_val, y_neg_mean);
    yy_prob=y_pos_prob * COND_NEG_PROB(x_val,y_val, x_neg_mean);

    xy_prob= max(x_pos_prob * COND_HET_PROB(y_val,x_val),
                 y_pos_prob * COND_HET_PROB(x_val,y_val));
}

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